Thermocapillary effects in driven dewetting and self-assembly of pulsed laser-irradiated metallic films

Agegnehu Atena  
*University at Buffalo*

Mikhail Khenner  
*Western Kentucky University, mikhail.khenner@wku.edu*

Follow this and additional works at: http://digitalcommons.wku.edu/math_fac_pub

Part of the Applied Mechanics Commons, Fluid Dynamics Commons, Materials Science and Engineering Commons, Nanoscience and Nanotechnology Commons, Non-linear Dynamics Commons, Numerical Analysis and Computation Commons, Partial Differential Equations Commons, and the Transport Phenomena Commons

**Recommended Repository Citation**  
**Available at:** http://digitalcommons.wku.edu/math_fac_pub/30

This Article is brought to you for free and open access by TopSCHOLAR®. It has been accepted for inclusion in Mathematics Faculty Publications by an authorized administrator of TopSCHOLAR®. For more information, please contact topscholar@wku.edu.
Thermocapillary effects in driven dewetting and self assembly of pulsed-laser-irradiated metallic films

A. Atena and M. Khenner

Department of Mathematics, University at Buffalo, SUNY, Buffalo, New York 14260, USA

(Received 14 October 2008; revised manuscript received 7 May 2009; published 3 August 2009)

In this paper the lubrication-type dynamical model is developed of a molten, pulsed-laser-irradiated metallic film. The heat transfer problem that incorporates the absorbed heat from a single beam or interfering beams is solved analytically. Using this temperature field, we derive the three-dimensional long-wave evolution partial differential equation for the film height. To get insights into dynamics of dewetting, we study the two-dimensional (2D) version of the evolution equation by means of a linear stability analysis and by numerical simulations. The stabilizing and destabilizing effects of various system parameters, such as the peak laser beam intensity, the film optical thickness, the reflectivity, and the Biot and Marangoni numbers, are elucidated. It is observed that the film stability is promoted for such parameter variations that increase the heat production in the film. In the numerical simulations the impacts of different irradiation modes are investigated. In particular, we obtain that in the interference heating mode the spatially periodic irradiation results in a spatially periodic film rupture with the same or nearly equal period. The 2D model qualitatively reproduces the results of the experimental observations of a film stability and spatial ordering of a resolidified nanostructures.

DOI: 10.1103/PhysRevB.80.075402

PACS number(s): 81.16.Dn, 47.54.Jk, 47.55.nb, 81.16.Rf

I. INTRODUCTION

Studies of dewetting, rupture and pattern formation in thin liquid films are very important for advanced technologies and also present an interest for basic physical sciences. However, most experimental and theoretical results have been obtained for aqueous and polymer films.

In this paper we report on our modeling studies of a metallic film dewetting by pulsed-laser irradiation (PLI). In the experiments on laser-irradiated metal films by Bischof et al.,1 both generic scenarios of dewetting and rupture were observed, i.e., by the growth of surface perturbations (spinodal regime3–4) and by nucleation and growth of holes.5 Very recently, several groups reported the results of similar experiments on thinner films (thickness h ~ 3–25 nm) that are irradiated by a single pulsed beam7–11 as in Bischof et al.,1 as well as by two or more interfering pulsed beams [pulsed-laser interference irradiation (PLII)].12–14 These experiments indicate that dewetting in such films is primarily spinodal.

The process of dewetting is analyzed in the cited papers using a thermal transport modeling7,10,12 and the standard isothermal thin-film partial differential equation (PDE).8,15 The consensus is that dewetting is driven by a long-range intermolecular (van der Waals) forces and the thermocapillary forces, with negligible material evaporation. Most interestingly, in the PLII mode the same static interference picture is formed on the film surface at each pulse (i.e., the alternating lines of the hot and cold regions in two-beam PLII, or the rectangular grid of the hot and cold lines in four-beam PLII). Through the thermocapillary fluid flow such lateral spatial nonuniformity of the temperature field allows the fabrication of one- and two-dimensional (2D) lattices of metal nanoparticles.

While the general picture has been laid out quite clear in the cited papers, there have been no attempts to develop a consistent PDE-based model of dewetting in a metallic film system, which incorporates thermocapillarity and the spatial and temporal nonuniformities due to laser irradiation. Presentation of such model is the subject of this paper. The model allows the studies of dewetting, rupture and nanopatterning in three-dimensional (3D) films for a set of laser parameters, such as the pulse shape and repetition frequency, the power intensity of the radiation, the arrangement and separation distance of the interference fringes, and the strength of interference. Our modeling attempts to capture the general features and trends of the dewetting process for the very special material systems and heating conditions. The model is applicable to thin films of nonreactive metals including Co, Fe, Au, Ni, Cu, Ag, and Mo on SiO2/Si substrates. The experimental papers cited above demonstrate that generic features of the nanoscale dewetting process under pulsed-laser heating are very similar for all combinations of these metals and substrates. For our analyses and simulations we take the material parameters values that closely mimic the Co/SiO2 system8–11,13,14 (see Table I). Most parameters are taken directly from these papers. Some parameters [the optical-absorption coefficient, laser peak intensity, heat transfer coefficients, second Hamaker constant (\(\tilde{B}\))] are estimated given the material system and the heating regime; true values may deviate within one or two orders of magnitude from the adopted values. However, these parameters enter the model in combinations with other physical parameters through the dimensionless quantities (Table II), many of which we vary in broad intervals about the most typical values in order to demonstrate their effects. Also it must be noted that some values (such as the heat capacity and thermal conductivity) are taken for solid Co since our search of published and Internet databases for values specific to liquid Co did not yield results. However, very small differences are expected.

We emphasize that the influence of radiative heating on fluid dynamics was theoretically studied only in a handful of papers.16–21 Most notably, Oron and Peles19 studied thermocapillary flows and instabilities of evaporative thin aq...
ous films with constant internal heat generation. Oron\textsuperscript{20} expanded this study to the case of irradiation by a single continuous-wave laser beam. Grigoriev\textsuperscript{21} analyzed mechanisms of passive and active feedback control of evaporatively driven instabilities in irradiated thin films. The primary conclusion of these studies, which are based on long-wave theory, is that irradiation can partially suppress the growth of instabilities. Also, Ajayev\textsuperscript{16} studied axisymmetric dewetting and rupture, in a molten state, of a thin metallic film, which has been melted by a single energetic laser pulse with a Gaussian spatial shape. They accounted for evaporation and long-range intermolecular attraction to the substrate and identified the thermocapillary stresses as the major driving force of a film evolution. It must be noted that neither of these papers considers uniform irradiation or the film reflectivity. The latter, as has been pointed out in Refs.\textsuperscript{9} and \textsuperscript{10}, is often the quantity of key importance for the dynamics of the ultrathin metallic films.

This paper is organized as follows. In Sec. II we formulate the equations of fluid motion for a film irradiated by PLI or PLII and then obtain the temperature field in the long-wave approximation. Using this field, we derive the 3D long-wave evolution PDE for the surface height. In Sec. III we perform the linear stability analysis of the 2D surface of the film and the numerical simulations of the 2D surface dynamics. We show how the surface stability, surface shape, rupture time and nanostructure array formation are affected by key dimensionless parameters, such as the film optical thickness, peak laser beam intensity, number of incident pulses and their duration, Marangoni and Biot numbers, and by the general spatial nonuniformity of the heat production in the PLII mode. Also we compare the qualitative and quantitative characteristics of stability and dewetting in the systems with zero and nonzero reflectivity. Sec. IV contains the discussion and conclusions.

### II. DERIVATION OF THE TEMPERATURE FIELD AND EVOLUTION EQUATION

In the PLI or PLII experiments, the solid film is periodically melted by a laser pulse. Following Refs.\textsuperscript{1} and \textsuperscript{8–14} we disregard periodic cycles of the melt resolidification between laser pulses and assume, for the purpose of the analysis and nonlinear dynamical simulations of the dewetting process, that the metallic film is always in the molten (i.e., liquid) state. This is reasonable since it has been shown that the mass transport in the solid state is negligible compared to the one in the liquid state, and so is the film deformation. \textsuperscript{8} In other words, our model assumes that between the laser pulses the film cools down to the temperature that is just above the solidification temperature, and thus it always stays liquid. Correspondingly, the dewetting process is treated as a continuous one in simulations.

Thus we assume a thin film of an incompressible Newtonian liquid lying on a planar horizontal substrate. The mean height of the film, $H$, is assumed much smaller than the lateral dimension $L$, thus $H/L = \varepsilon \ll 1$. The surface tension $\sigma$ is a linear function of the temperature $\tilde{T}$,

$$\sigma = \sigma_m - \tilde{\gamma}(\tilde{T} - \tilde{T}_m), \quad \tilde{T} > \tilde{T}_m. \tag{1}$$

Here $\tilde{T}_m$ is the melting temperature of the film, $\sigma_m$ is the surface tension at the melting temperature, and $\tilde{\gamma} = -\frac{\partial \sigma}{\partial T} > 0$.

### TABLE I. Material parameters.

<table>
<thead>
<tr>
<th>Physical parameter</th>
<th>Typical values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Film thickness ($H$)</td>
<td>10 nm</td>
</tr>
<tr>
<td>Optical absorption coefficient ($\delta$)</td>
<td>$10^8$ m$^{-1}$</td>
</tr>
<tr>
<td>Film density ($\rho$)</td>
<td>$8.92 \times 10^3$ Kg/m$^3$</td>
</tr>
<tr>
<td>Heat capacity ($c_p$)</td>
<td>420 J/Kg K</td>
</tr>
<tr>
<td>Thermal conductivity (film) ($\kappa$)</td>
<td>100 W/m K</td>
</tr>
<tr>
<td>Thermal diffusivity ($\chi$)</td>
<td>$2.675 \times 10^{-5}$ m$^2$/s</td>
</tr>
<tr>
<td>Melting temperature ($\tilde{T}_m$)</td>
<td>1768 K</td>
</tr>
<tr>
<td>Ambient temperature ($\tilde{T}_a$)</td>
<td>300 K</td>
</tr>
<tr>
<td>Substrate temperature ($\tilde{T}_s$)</td>
<td>1900 K</td>
</tr>
<tr>
<td>Acceleration of gravity ($g$)</td>
<td>9.8 m/s$^2$</td>
</tr>
<tr>
<td>Dynamic viscosity ($\mu$)</td>
<td>$4.45 \times 10^{-3}$ Pa-s</td>
</tr>
<tr>
<td>Surface tension at melting point ($\sigma_m$)</td>
<td>1.88 J/m$^2$</td>
</tr>
<tr>
<td>$\tilde{\gamma}$ (at melting point)</td>
<td>$5 \times 10^{-6}$ J/K m$^2$</td>
</tr>
<tr>
<td>Characteristic velocity ($U = \tilde{\mu}/\rho H$)</td>
<td>50 m/s</td>
</tr>
<tr>
<td>Laser peak intensity ($I$)</td>
<td>$10^{10}$ W/m$^2$</td>
</tr>
<tr>
<td>Heat transfer coefficient ($\alpha_I$)</td>
<td>$1.41 \times 10^4$ W/m$^2$ K</td>
</tr>
<tr>
<td>Heat transfer coefficient ($\alpha_s$)</td>
<td>$\geq 1$ W/m$^2$ K</td>
</tr>
<tr>
<td>Hamaker constant ($\tilde{A}$)</td>
<td>$1.41 \times 10^{-18}$ J</td>
</tr>
<tr>
<td>Hamaker constant ($\tilde{B}$)</td>
<td>$2.6 \times 10^{-13}$ N</td>
</tr>
<tr>
<td>Substrate thickness ($H_s$)</td>
<td>10 nm</td>
</tr>
<tr>
<td>Substrate thermal conductivity ($\kappa_s$)</td>
<td>1.3 W/m K</td>
</tr>
</tbody>
</table>

### TABLE II. Dimensionless parameters.

<table>
<thead>
<tr>
<th>Dimensionless group</th>
<th>Definition</th>
<th>Typical values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scaling parameter ($\varepsilon$)</td>
<td>$H/L$</td>
<td>0.01</td>
</tr>
<tr>
<td>Reynolds number (Re)</td>
<td>$\rho U H / \mu$</td>
<td>1</td>
</tr>
<tr>
<td>Brinkman number (Br)</td>
<td>$\mu U^2 / H \kappa$</td>
<td>0.11</td>
</tr>
<tr>
<td>Peclet number (Pe)</td>
<td>$\rho c_p U H / \kappa$</td>
<td>0.019</td>
</tr>
<tr>
<td>Capillary number ($C$)</td>
<td>$\mu U / \sigma$</td>
<td>0.1184</td>
</tr>
<tr>
<td>Gravity parameter ($G$)</td>
<td>$\rho g H^2 / \mu U$</td>
<td>$3.93 \times 10^{-13}$</td>
</tr>
<tr>
<td>Biot number ($\beta$)</td>
<td>$\alpha_H / \kappa$</td>
<td>$10^{-6}$</td>
</tr>
<tr>
<td>Biot number ($\tilde{\beta}$)</td>
<td>$\alpha_H / \kappa$</td>
<td>$10^{-6}$</td>
</tr>
<tr>
<td>Surface tension ($\sigma_m$)</td>
<td>$\varepsilon \sigma_m / \mu U$</td>
<td>0.084</td>
</tr>
<tr>
<td>Marangoni number ($M$)</td>
<td>$\varepsilon H \tilde{\gamma} / 2 \mu U \kappa$</td>
<td>$1.125 \times 10^{-5}$</td>
</tr>
<tr>
<td>Hamaker constant ($A$)</td>
<td>$\tilde{A}/6 \pi \mu U H^2$</td>
<td>$3.37 \times 10^{-5}$</td>
</tr>
<tr>
<td>Hamaker constant ($B$)</td>
<td>$\tilde{B}/\mu U H$</td>
<td>$1.17 \times 10^{-6}$</td>
</tr>
<tr>
<td>Melting temperature ($\tilde{T}_m$)</td>
<td>$\tilde{\kappa} \tilde{T}_m / \tilde{H}$</td>
<td>1768</td>
</tr>
<tr>
<td>Ambient temperature ($\tilde{T}_a$)</td>
<td>$\tilde{\kappa} \tilde{T}_a / \tilde{H}$</td>
<td>300</td>
</tr>
<tr>
<td>Substrate temperature ($\tilde{T}_s$)</td>
<td>$\tilde{\kappa} \tilde{T}_s / \tilde{H}$</td>
<td>1900</td>
</tr>
<tr>
<td>Optical thickness ($D$)</td>
<td>$\tilde{\delta} \tilde{H}$</td>
<td>1</td>
</tr>
<tr>
<td>Substrate thickness ($h_s$)</td>
<td>$H_s / \tilde{H}$</td>
<td>1</td>
</tr>
<tr>
<td>Ratio of thermal conductivities ($\tilde{\Gamma}$)</td>
<td>$\kappa_s / \kappa$</td>
<td>$1.3 \times 10^{-2}$</td>
</tr>
<tr>
<td>Prefactor, reflectivity function ($r_0$)</td>
<td>Exponent, reflectivity function ($a_r$)</td>
<td>0.44</td>
</tr>
</tbody>
</table>
The tildes mark dimensional quantities. The governing equations of the melt are the Navier-Stokes, continuity, and the energy equations,

\[ \rho \left( \mathbf{v} + (\nabla \cdot \mathbf{v}) \right) = \mathbf{\bar{v}} \cdot \mathbf{\bar{\Omega}} + \rho \mathbf{g}, \]  

\[ \mathbf{\bar{v}} \cdot \mathbf{v} = 0, \]  

\[ \rho c_p (\mathbf{\bar{T}}_t + \mathbf{v} \cdot \nabla \mathbf{\bar{T}}) = \kappa \nabla^2 \mathbf{\bar{T}} + \tau_{ij} \frac{\partial u_j}{\partial x_i} + \bar{Q}, \]  

where \( \mathbf{\bar{v}} = (\mathbf{\bar{u}}, \mathbf{\bar{v}}, \mathbf{\bar{w}}) = (\mathbf{\bar{u}}_1, \mathbf{\bar{u}}_2, \mathbf{\bar{u}}_3) \) is the velocity field, \( \mathbf{\bar{\Omega}}_{ij} = -\mathbf{\bar{\tau}}_{ij} \) is the full stress tensor for incompressible fluid, \( \mathbf{\bar{\tau}}_{ij} = \mu \left( \frac{\partial x_i}{\partial x_j} + \frac{\partial x_j}{\partial x_i} - \frac{2}{3} \right) \) is the viscous stress tensor, \( \mu \) is the dynamic viscosity, \( \rho \) is the density, \( \mathbf{g} \) is the gravitational acceleration, and \( \bar{Q} \) is the internal heat source. The internal heat generation is due to the absorption of radiation from the monochromatic laser beam. We assume that the free surface of the film is optically smooth, nonscattering, and nonemissive.

Under the stated assumptions the form of the heat source term is given by Bouguer’s law, \[ \bar{Q} = \frac{\delta (1 - R(h))}{2} f(\mathbf{x}, \bar{y}, \bar{t}) \exp(\delta(z - h)), \]  

where \( I \) is the laser power intensity, \( \delta \) is the spatially uniform optical-absorption coefficient, \( h \) is the position of the free surface, \( R(h) \) is reflectivity, and \( f(\mathbf{x}, \bar{y}, \bar{t}) \) is a positive function with mean value one whose functional form depends on the interference mode and the temporal shape of the laser pulse.

The boundary conditions at the free surface \( z = \bar{h}(\mathbf{x}, \bar{y}, \bar{t}) \) are:

(i) the normal and shear stress balances,

\[ \mathbf{n} \cdot \mathbf{\bar{\Omega}} = -\bar{\sigma} \nabla \cdot \mathbf{n} + \mathbf{\bar{\Pi}}, \]  

\[ \mathbf{t} \cdot \mathbf{\bar{\Omega}} = -\mathbf{\bar{t}} \cdot \nabla \mathbf{n}, \]  

where \( \mathbf{n} \) is the unit outward normal to the surface, \( \mathbf{t} \) is the unit tangent vector, and \( \mathbf{\bar{\Pi}} \) is the disjoining pressure. The latter is specified in the form \( \mathbf{\bar{\Pi}} = (A \cdot \delta) \bar{h}^{-3} + \bar{B} \bar{h}^{-2} \) where \( A \) and \( B \) are the Hamaker constants. The first term is due to the dispersion (van der Waals) forces and the second term is due to the contributions from the kinetic energy of the electrons.

(ii) The kinematic condition,

\[ \bar{w} = \bar{h}_t + \bar{u} \bar{h}_x + \bar{v} \bar{h}_y, \]  

that balances the normal component of the liquid velocity with the speed of the interface;

(iii) the temperature boundary condition is given by the Newton’s law of cooling,

\[ \kappa \bar{T}_z = -\alpha_i (\bar{T} - \bar{T}_a), \]  

where \( \alpha_i \) is the heat transfer coefficient and \( \bar{T}_a \) is the air temperature.

The boundary conditions for velocity of the melt flow at the solid boundary \( z = 0 \) (the substrate) are no slip, \( \bar{u} = \bar{v} = 0 \), and no penetration, \( \bar{w} = 0 \). Two types of the temperature boundary condition at the substrate will be considered.

The boundary condition of the first type (TBC1) is the Newton’s law of cooling at \( z = 0 \),

\[ \kappa \bar{T}_z = \alpha_e (\bar{T} - \bar{T}_s), \]  

where \( \alpha_e \) is the heat exchange coefficient and \( \bar{T}_s \) is the temperature of the substrate. Note that the usual case of a fixed temperature at the solid boundary, \( \bar{T} = \bar{T}_s \) (which corresponds to perfectly conducting substrate), can be easily obtained. It suffices to take the limit \( \alpha_e \to \infty \) (or equivalently, the limit \( \beta \to \infty \), see the definition of \( \beta \) below) in the dimensionless expressions for the temperature and in the evolution PDE for the film height. It is clear from the form of these equations that this limit exists and that taking the limit results simply in some terms dropping out of the equations.

The boundary condition of the second type (TBC2) is the continuity of the temperature and the thermal flux at \( z = 0 \),

\[ \bar{T} = \bar{\theta}, \quad \kappa \bar{T}_z = \kappa_e \bar{\theta}_z, \]  

where \( \bar{\theta} \) is the temperature field in the substrate. The substrate is assumed thin, \( H_s \to H \) (where \( H_s \) is substrate thickness). Thus the temperature field \( \bar{\theta} \) can be derived in the lubrication approximation.

### A. Nondimensionalization

We use the following scalings to nondimensionalize the problem:

\[ \bar{x} = xL, \quad \bar{y} = yL, \quad \bar{z} = zH, \quad \bar{h} = hH, \quad \bar{u} = uU, \quad \bar{v} = vU, \quad \bar{w} = wU, \quad \bar{T} = (L/U) \bar{t}, \quad \bar{\theta} = (H/U \kappa) \bar{\theta}, \quad \bar{\tau} = (\mu U/eH) \bar{\tau}, \quad \mathbf{\bar{\Pi}} = (\mu U/eH) \mathbf{\bar{\Pi}}, \quad \bar{\alpha} = (\mu U/eH) \bar{\alpha}, \quad \bar{\gamma} = (\mu U/eH) \gamma, \quad \text{where} \ U \text{ is the characteristic flow velocity. Typical values of the material parameters are shown in Table I.} \]

### B. Temperature distribution in the film

Upon using the scalings, the dimensionless energy equation is

\[ e \mathbf{Pc} (\mathbf{\bar{T}}_t + u T_s + v T_y + w T_z) = T_{zz} + e^4 T_{xx} + T_{yy} + (D/2)(1 - R(h)) \exp(D(z - h)) + e^2 B (u_x^2 + u_y^2 + u_z^2 + v_x^2 + v_y^2 + w_z^2) + B (u_x^2 + v_y^2 + w_z^2), \]

where \( e = \rho c_p U H / \kappa \) is the Peclet number, \( B = \mu U^2 / H \) is the Brinkman number, and \( D = \partial H \) is the optical thickness of a film of the uniform thickness \( H \) for the incident radiation with the mean penetration length \( \delta^{-1} \). Using values of the material parameters from Table I gives \( e = 0.019 \leq 1 \) and

\[ 075402-3 \]
Thus in the leading order the energy equation is
\[ T_{zz} + (D/2)f(1 - R(h))\exp(D(z - h)) = 0, \]  
and the energy equation in the substrate is
\[ \theta_{zz} + (D/2)f \exp(D(z - h)) = 0. \]

The dimensionless boundary conditions for Eqs. (13) and (14) are
\[ z = h: \quad T_z = -\beta(T - T_s), \]
\[ z = 0: \quad T_z = \beta_s(T - T_s) \quad \text{(TBC1)}, \]
o or
\[ T = \theta, \quad T_z = \Gamma \theta \quad \text{(TBC2)}, \]
where \( \beta = \alpha H/\kappa \) and \( \beta_s = \alpha H/\kappa \) are the Biot numbers, \( \Gamma = \kappa/\kappa \) is the ratio of the thermal conductivity of the substrate to one of the film, and \( h = H/H \). Of course, boundary condition (18) is not needed when the boundary condition (TBC1) is used.

Solution of Eq. (13) subject to boundary conditions (15) and (16) or the solution of Eqs. (13) and (14) subject to boundary conditions (15), (17), and (18) gives the temperature field in the film,
\[
T(x,y,z,t) = \left\{ \frac{Y}{2} - \exp(-Dh) \left( \frac{Y}{2} + K \right) + K \exp[D(z - h)] + \frac{z}{2} \right\}
\times \left[ f(1 - R(h)] + T_s + \{T_a - T_s + F(h)f[1 - R(h)] \right]
\times (Y + z)\beta, \tag{19}
\]
where \( K = -1/2D \),
\[
F(h) = \frac{-Y}{2} + \exp(-Dh) \left( \frac{Y}{2} + K \right) - \frac{h}{2} - K, \tag{20}
\]
and \( Y = 1/\beta_s \) (TBC1), or \( Y = h_s/\Gamma \) (TBC2). Note that Eq. (19) results upon the linearization in \( \beta \) of the full solution of the problem. This is warranted since \( \beta \ll 1 \) (see Table II).

Substitution \( z = h \) in Eq. (19) gives the temperature at the free surface,
\[
T^{(b)} = T(x,y,h,t) = T_s - F(h)f(1 - R(h)) + (Y + h)(F(h)f(1 - R(h)) + T_a - T_s)\beta. \tag{21}
\]

In Figs. 1 and 2 we show the typical contour plots of the temperature field in the film of the uniform dimensionless height \( h = 1 \) at a vertical cross section in the middle of the domain. These figures were obtained with (TBC1), \( R(h) = 0 \) and (TBC2), \( R(h) \neq 0 \), respectively. [Remarks: the form of the reflectivity function \( R(h) \) is shown in Eq. (22) below. Unless noted otherwise in the text or in a figure caption, the parameter values that are used to obtain all figures in the paper are taken from Table II. Also, the dimensionless quantities are plotted in all figures except Figs. 8 and 11.] In the top row of Figs. 8 and 11, the film surface is heated by the uniform (spatially and temporally) laser beam. Bottom row: the surface is heated by the spatially uniform but spatially nonuniform laser beam. Left panel: optically thick film. Right panel: optically thin film. Notice very small vertical temperature gradient in all cases \((\partial T/\partial z > 0)\).

If the optical thickness \( D \ll 1 \) the radiation passes through the film and such films are called optically thin or transpar-
ent. If $D \gg 1$ the radiation penetrates only into a very thin boundary layer adjacent to the free surface of the film and in this case the film is called optically thick or opaque. Note that in the dimensionless energy equation [Eq. (13)] $\tilde{F}$ characterizes the variation of the heat source in a horizontal plane, whereas the function $a(z) = \exp(D(z-h))$ describes its dependence on the depth of the film, $z$. Since $0 \leq z \leq h$, $a(z)$ is the increasing function of the height $z$; however, for the optically thin film the difference $a(h)-a(0)$ is a small quantity. In other words, the top and the bottom of the film receive approximately same energy from the laser beam. As a result the temperature difference across the film is small (see the right panels of Figs. 1 and 2). On the other hand, the bottom part of the optically thick film receives less energy from the laser beam than the top part, which makes the temperature difference across the film larger (see the left panels of Figs. 1 and 2).

Before we proceed further, we state the dimensionless form of the effective film reflectivity that we use in the paper. We assume the following form after Refs. 9 and 10:

$$R(h) = r_0(1 - \exp(-a_r h)),$$  

where $r_0$ and $a_r$ are the material dependent parameters (see Table II).

### C. Derivation of the evolution equation for the film height

In this section we outline the conventional procedure of the derivation of the evolution equation.

The dimensionless Navier-Stokes and continuity equations read

$$\epsilon\Re(\eta + \eta u_x + v \eta u_y + \eta u_z) = -p_z + \epsilon^2(u_{xx} + u_{yy}) + u_{zz},$$

$$\epsilon^2\Re(u_x + \eta u_x + v u_y + \eta u_z) = -p_x + \epsilon^2(v_{xx} + v_{yy}) + v_{zz},$$

$$\epsilon^3\Re(w_x + \eta w_x + v w_y + \eta w_z) = -p_x + \epsilon^2(w_{xx} + w_{yy}) + w_{zz} - G,$$

$$u_x + v_y + w_z = 0,$$  

where $\Re = \rho U h / \mu$ is the Reynolds number (which is of order one in magnitude for the case considered here), and $G$ is the gravity number. In the leading order the Navier-Stokes and continuity equations read as

$$p_x = u_{zz}, \quad p_y = v_{zz}, \quad p_z = -G,$$  

$$u_x + v_y + w_z = 0.$$  

Using the long-wave approximation, $|h_x|, |h_y| \ll 1$ and the usual assumption of large surface tension, $\tilde{C} = \epsilon^2 C^{-1}$ (where $C$ is the capillary number) in Eq. (6), the dimensionless normal stress balance condition is

$$-p = \tilde{C}(h_{xx} + h_{yy}) + A h^2 + B h^3,$$  

where $A$ and $B$ are the dimensionless Hamaker constants. The dimensionless shear stress balance condition reads as

$$u_z = \sigma_x + h_1 \sigma_z, \quad v_z = \sigma_y + h_2 \sigma_z,$$  

where the dimensionless surface tension is given by $\sigma = \sigma_m - \gamma(T - T_m)$.

Taking the cross-sectional averages of $u$ and $v$ over the film height and integrating Eq. (26) using the no-slip condition, we obtain a more convenient form of the kinematic boundary condition,

$$h_1 + (h_1 u)_x + (h_1 v)_y = 0.$$  

Integrating the first two equations in Eq. (25) twice in $z$ and applying the no-slip boundary condition yields

$$u = \left(\frac{z^2}{2} - h_z\right)p_x + z u_{zz}|_{z=h},$$

$$v = \left(\frac{z^2}{2} - h_z\right)p_y + z v_{zz}|_{z=h}.$$  

Cross-sectional averaging of Eq. (30) results in

$$\overline{u} = \frac{1}{h} \int_0^h udz = -\frac{h^2}{3}p_x + \frac{h}{2}u_{zz}|_{z=h},$$

$$\overline{v} = \frac{1}{h} \int_0^h vdz = -\frac{h^2}{3}p_y + \frac{h}{2}v_{zz}|_{z=h}.$$  

Since $u_z$ and $v_z$ are expressed in terms of the derivatives of the surface tension [Eq. (28)], which in turn is expressed in terms of the derivatives of the temperature at the free surface, we need to calculate the latter derivatives. Hence, by differentiating Eq. (19) and evaluating the derivatives at $z = h$ we find

$$T^{(i)}_{x(y)} = f(1-R(h))(1-\beta(h + Y))F_i(h)h_{x(y)}$$

$$+ fR(h)(1-\beta(h + Y))F(h)h_{x(y)} - f(h)(1-R(h))f_{x(y)}\beta,$$  

$$T^{(i)}_z = \beta(f(1-R(h))F(h) + T_a - T),$$  

where

$$F_i(h) = \frac{1}{2} + \frac{1}{2}(YD - 1)\exp(-Dh),$$  

and the prime denotes differentiation. Substituting Eq. (33) in Eq. (28) through the derivatives of $\sigma$ and using Eq. (27) in Eqs. (31), the expressions for the average velocities become

$$\overline{u} = -\frac{G h^2}{3}h_x + \frac{\tilde{C} h^2}{3}(h_{xxx} + h_{yyy}) + \left(\frac{A}{h^2} - \frac{2B}{3h} - M h T^{(i)}_x\right)h_x$$

$$- M h T^{(i)}_x + O(\beta f),$$

$$\overline{v} = -\frac{G h^2}{3}h_y + \frac{\tilde{C} h^2}{3}(h_{xxx} + h_{yyy}) + \left(\frac{A}{h^2} - \frac{2B}{3h} - M h T^{(i)}_y\right)h_y$$

$$- M h T^{(i)}_y + O(\beta f),$$

where $M = \gamma / 2$ is the Marangoni number.
Finally, substituting Eq. (35) in kinematic boundary condition (29) and using Eq. (33) result in the evolution equation for the film height,
\[ h_t = \nabla \cdot \left[ -\frac{\hat{c}}{3} h^3 \nabla^2 h + \frac{G}{3} h^3 \nabla h - \left( \frac{A}{h} - \frac{2B}{3} \right) h \right. \]
\[ + M \beta (T_a - T_s) h^2 \nabla h + M F_1(h)(1 - R(h)) h^2 \nabla h \]
\[ + 3 M R'(h) F(h) h^2 \nabla h - M \beta (T_a - T_s) h^2 \nabla h \]
\[ + M \beta f(1 - R(h))(F(h) - (h + Y) F_1(h)) h^2 \nabla h \]. \quad (36)

In the following sections of the paper, we assume the laser irradiation either uniform in the xy plane, or nonuniform only in the x direction. The former situation corresponds to the PLI case, i.e., one of a single incident laser beam, where the interference is absent. If there is only one beam, we approximate its spatial intensity distribution on irradiated domain by a constant, i.e., \( f = 1 \) or \( f = f(0) \). The latter situation corresponds to two-beam PLII. In both cases the simpler 2D model provides valuable insight into the dynamics of dewetting. This model is studied in Sec. III.

It must be noted that in Eq. (36) we omitted the term \( -M(1 - R(h)) \nabla \cdot [F(h) h^2 \nabla f] \) and the similar term proportional to the small parameter \( \beta \). In PLII, when \( f \) is nonuniform in the plane [see Eq. (43)], the omitted terms describe the surface shape change by thermocapillarity due to in-plane temperature equilibration by heat conduction. In the PLII experiments the in-plane heat fluxes are negligible between the interference fringes is much larger than the film thickness. Thus the lateral temperature profile is approximately static; i.e., it is determined by the geometrical arrangement of the interference fringes. A few sample computations that we performed with Eq. (36), where the omitted terms are present, show that these terms are indeed much smaller than the other terms, and their influence on the film dynamics is negligible. This can be also understood by noticing that in the experiment (and, correspondingly, in our modeling) the wave number of the surface perturbation, \( k \), is larger or much larger than the wave number, \( q \), of the spatially modulated laser light field \( f \). See, for example, Fig. 12, which is obtained with \( k = 2.2 \) and \( q = 0.157 \). Thus \( \nabla f \sim q f \ll \nabla h \sim kh \), and the terms proportional to \( \nabla f \) are smaller than the terms proportional to \( \nabla h \).

### III. 2D MODEL OF FILM DYNAMICS

The 2D reduction of evolution Eq. (36) reads as
\[ h_t = \left\{ -\frac{\hat{c}}{3} h^3 \nabla^2 h + \frac{G}{3} h^3 \nabla h - \left( \frac{A}{h} - \frac{2B}{3} \right) h \right. \]
\[ + M \beta (T_a - T_s) h^2 \nabla h + M F_1(h)(1 - R(h)) h^2 \nabla h \]
\[ + 3 M R'(h) F(h) h^2 \nabla h - M \beta (T_a - T_s) h^2 \nabla h \]
\[ + M \beta f(1 - R(h))(F(h) - (h + Y) F_1(h)) h^2 \nabla h \right\} , \quad (37)

### A. Linear stability analysis

For the purpose of the linear stability analysis, we assume uniform laser power intensity distribution \( f = 1 \) and a small normal perturbation of the uniform base state, \( h = h^{(0)} + \xi(x, t) = 1 + e^{i\omega t} e^{ikx} \), where \( h^{(0)} \) equals to one due to nondimensionalization and \( \omega \) represents the growth rate of the perturbation having a wave number \( k \). Linearizing Eq. (37) in \( \xi \) results in the dispersion relation
\[ \omega(k) = -\frac{G}{3} k^2 - \frac{\hat{c}}{3} k^4 + \left( A - \frac{2B}{3} \right) k^2 - M \beta (T_a - T_s) k^2 \]
\[ + MR'(1)(F(1)(-1 + \beta (1 + Y)) k^2 \]
\[ + M(1 - R(1))(F(1)(-1 + \beta (1 + Y)) F_1(1)) k^2 \]. \quad (38)

From Eq. (38) we find the critical wave number \( k_c \), such that \( \omega > 0 \) for \( 0 < k < k_c \).
\[ k_c = \left[ \frac{3}{\hat{c}} \left( -\frac{G}{3} + A - \frac{2B}{3} - M \beta (T_a - T_s) \right. \right. \]
\[ \left. + M R'(1)(F(1)(-1 + \beta (1 + Y)) \right. \]
\[ \left. + M(1 - R(1))(F(1)(-1 + \beta (1 + Y)) F_1(1)) \right) \left[ \frac{1}{2} \right] \]. \quad (39)

The growth rate \( \omega \) attains its maximum value \( \omega_{\max} \) at the wave number \( k_m = k_c / \sqrt{2} \), which is usually referred to as the “most dangerous mode.”

The terms at the right-hand side of Eq. (38) describe the stabilizing effect of gravity, the stabilizing effect of capillary forces, the destabilizing and stabilizing effects of the van der Waals component and the electronic component of the disjoining pressure, respectively, the stabilizing effect of the temperature gradient across the film, if \( T_a > T_s \), and destabilizing effect otherwise, and the last two terms are due to the volumetric heat source. The coefficient of the last two terms in Eqs. (38) and (39), \( M R'(1)(F(1)(-1 + \beta (1 + Y)) + M(1 - R(1))(F(1)(-1 + \beta (1 + Y)) F_1(1)) \) is negative for the typical parameters values from Table II and for all values of \( D \). This holds true for both cases of the boundary conditions [(TBC1) or (TBC2)] and does not depend on the presence of film reflectivity (see Figs. 5 and 6). Thus the term associated with the heat source has a stabilizing impact.\(^{19-21}\)

1. Results for the case (TBC1) and \( R(h) = 0 \)

In this section \( Y = 1 / \beta \), and \( r_0 = 0 \) in Eq. (22). The typical graphs of \( \omega(k) \) are shown in Fig. 3. The solid curve represents \( \omega(k) \) calculated with all terms at the right-hand side of Eq. (38) and the dash-dot curve shows \( \omega(k) \) computed without the last term. [The fifth term is automatically zero since \( R'(1) = 0 \) due to \( R(h) = 0 \).] As expected both the maximum growth rate and the cutoff wave number in the former case are smaller than the corresponding quantities in the latter case.

The Marangoni effect is expressed by the two components, one responsible for the destabilizing thermocapillary...
effect [the fourth term in Eq. (38) with $T_c < T_s$, see Table II], and another responsible for the stabilizing effect associated with the heat source (the fifth term). Figure 4 shows the Marangoni effect when the stabilizing component is absent (left panel) and when both components are present (right panel). Since the Marangoni number $M$ increases with the peak intensity $I$, the irradiation of the film with a high intensity laser has stabilizing influence (below the onset of evaporation).

The impact of the optical thickness $D$ on the stability of the perturbation is shown in Fig. 5. It can be seen that $k_c$ and $\omega_{max}$ both decrease as $D$ increases, while the magnitude of the stabilizing effect (i.e., the coefficient) increases with $D$. Thus in agreement with Refs. 19–21, as the film becomes more opaque the internal heat generation increases and the associated Marangoni effect stabilizes the film.

Finally, we discuss impacts of $\beta_s$ and $\beta$. The cutoff wave number increases as $\beta_s$ increases ($k_c \approx 3.1099$ for $\beta_s=1$ and $k_c \approx 3.2257$ for $\beta_s=10^4$) approaching the constant value $\approx 3.23$ as $\beta_s \rightarrow \infty$. The maximum growth rate is very insignificantly affected by the change of $\beta_s$, increasing slowly and approaching value $7.65 \times 10^{-5}$ as $\beta_s \rightarrow \infty$. Thus the film is more stable for smaller $\beta_s$. Similarly, the cutoff wave number $k_c$ and the maximum growth rate increase insignificantly with increasing $\beta$ (while $\beta$ is kept typically small, as required by Table II). Clearly, as $\beta$ or $\beta_s$ increase the amount of heat in the film decreases due to heat losses to the ambient, and the film becomes less stable.

2. Results for the case (TBC2) and $R(h) \neq 0$

In this section $Y = h_s / \Gamma$ and $r_0=0.44$ in Eq. (22). The coefficient of the two stabilizing terms in the growth rate equation (38) is plotted in Fig. 6. Unlike Fig. 5, the dependence of the coefficient on $D$ is nonmonotone for both zero and nonzero reflectivities when the heat conduction in the thin substrate is taken into account. The maximum stabilization occurs in films with $D \sim 1$, and the minimum one in films with $D \ll 1$ or $D \gg 1$.

The corresponding maximum growth rate and the cutoff wave number are shown in Fig. 7. As $D$ starts to increase from zero, the film becomes more stable. In the interval...
greater than \( a \), (see also Refs. 9 and 10). This is the reason why the film temperature increases as the film thickness increases.

**B. Nonlinear evolution of the film**

The 2D evolution equation for the film height [Eq. (37)] is solved numerically using the method of lines. Integration in time is performed using the ODE solver RADAU whereas the discretization in space is carried out in the conservative form using the positivity-preserving\(^{26}\) second-order-accurate finite differencing on a spatially uniform staggered grid.

The perturbation

\[
h(x,0) = 1 + A_0 \cos(k_m x),
\]

where \( A_0 \) is the small amplitude and \( k_m \) is the wave number of the fastest growing instability as identified in the linear stability analysis, is imposed as the initial condition. Equation (37) is solved in the spatial domain \( 0 \leq x \leq 2n \pi/k_m \) (where \( n \) is an integer) subject to the periodic boundary conditions.

We performed simulations using different forms of \( f(x,t) \) that characterize the spatiotemporal power intensity distribution of the PLI or PLII at the film surface.

Firstly, we assume \( f \) uniform in both time and space; i.e., \( f=1 \). This corresponds to a steady heating of the film surface by a single laser beam with a uniform spatiotemporal shape. The results of the nonlinear simulations in this regime can be compared to the linear stability analysis in the previous section.

Next, with \( f \) still spatially uniform we assign a Gaussian temporal shape to \( f \) so that

\[
f(t) = e^{-(t-T/2)^2/2\sigma^2} \]

for a single pulse laser irradiation, and

\[
f(t) = \sum_{k=0}^{N-1} e^{-(t-(2k+1)T/2)^2/2\sigma^2} \]

for a sequence of \( N \) pulses of irradiation, where \( T \) is the pulse duration and \( \sigma \) is the standard deviation. (Note that \( d = 2\sigma\sqrt{2} \ln 2 \) is the Gaussian full width at half maximum.) Both situations again correspond to heating of the film surface by a single laser beam.

Finally, we consider the case of the two-beam interference. The two-beam interference produces a spatially modulated light field having the form\(^{12}\)

\[
f(x) = 1 + \alpha \cos \left( \frac{\pi}{k_m} \left( x - \frac{\pi}{k_m} \right) \right),
\]

where the parameter \( 0 < \alpha < 1 \) models the strength of the interference and \( 2\pi/q = \ell \) is the distance between two neighboring interference fringes. This distance \( \ell \) is given by \( \ell = \lambda/2 \sin(\theta/2) \), where \( \lambda \) is the wavelength of the primary laser beam and \( \theta \) is the angle between the two interfering beams. Note that the subtraction of \( \pi/k_m \) from \( x \) is to make the beam focused at the center of the domain.

Below we show the numerical results for the case (TBC1) and zero reflectivity. The numerical simulations for the case

**FIG. 7.** Variation in \( \omega_{max} \) (top row) and \( k_c \) (bottom row) with \( D \). Dot curve: \( R(h)=0 \); solid curve: \( R(h) \neq 0 \). The dot curve is included for comparison.

**FIG. 8.** Plot of the maximum dimensional film temperature vs film height. Dot curve: \( R(h)=0 \); solid curve: \( R(h) \neq 0 \). The dot curve is included for comparison.

075402-8
The TBC2 and $R(h) \neq 0$ give similar shape profiles. The inclusion of the reflectivity in the simulation makes the rupture time of the film shorter. In this sense the film is more unstable when $R(h) \neq 0$. We discuss this issue in more detail at the end of this Section.

C. Impacts of the different modes of irradiation

$f=1$. Figure 9 shows the evolution of the film surface resulting from uniform irradiation, both in time and space, by a single laser beam. The minimum point of the initial film surface goes further down and touches the substrate. In the simulation, the nonlinear dynamics of the film is followed until its minimum height gets a very small value (0.001) and then the film is said to be ruptured. Favazza et al. estimated the rupture time $T_r$ of a film (i.e., the time scale of dewetting) as $\bar{T}_r = 2\pi/\omega(k_m)$. For a 10-nm-thick film their calculation gives $\bar{T}_r \approx 1.25$ ms. Our linear stability analysis gives $\bar{T}_r \approx 1.9$ ms. Note that $\bar{T}_r$ depends on the amplitude of the initial surface perturbation. Naturally, perturbations with larger initial amplitude rupture the film faster. In the nonlinear dynamical simulation shown in Fig. 9 the rupture time for $A_0 = 0.01375$ is approximately 0.9 ms, which corresponds to the dimensionless time $\bar{T}_r = 43150$. It is seen in Fig. 10 that at the initial stage of the irradiation the nonlinear instability growth rate matches the one predicted by the linear stability analysis, but towards the end of the simulation the nonlinear instability grows much faster. This can be explained by observing that when the film height gets small the factor $A/h$ in Eq. (37) becomes very large, signaling that the destabilizing van der Waals component of the disjoining pressure dominates over stabilizing forces, which results in a faster instability growth. We also noticed that smaller values of the capillary number, $C$, sometimes result in a ring rupture, meaning that the film surface touches the substrate some distance from the vertical line through the minimum of the perturbation. Such rupture leaves behind an array of small liquid drops.\(^{16}\)

$f$ as in Eq. (41). The shape profile obtained by irradiating the surface with a single pulse of width $\delta = 10787$ (200 µs dimensional pulse width) is similar to the one resulting from uniform laser beam heating (Fig. 9). However, $T_r = 35138$ in this case, which is less than the rupture time for the uniform heating. The reason is that the energy absorbed from the Gaussian beam is less than the energy absorbed from the uniform irradiation, which causes the rapid growth of the instability leading to fast rupture.

$f$ as in Eq. (42). In this simulation we use several sequences of Gaussian pulses. In each sequence, pulses have same width and also the repetition frequency of pulses is same for all sequences. Figure 11 shows the rupture time vs pulse width. The surface morphology is similar to the one obtained by uniform laser beam heating. It can be seen that the rupture time increases as the pulse width increases. Again, this is because the energy generated from a narrower pulse is smaller than the energy generated from a wider pulse, and this increases the growth rate of the instability. Heating the film surface with wider pulses also require more number of pulses for the film to rupture. For example, 3064 pulses are enough to get the film ruptured when irradiated with a 1ns pulse, compared to 3293 pulses required for a 50ns pulse irradiation. It must be noted here that in any irradiation mode the rupture time increases approximately linearly with the peak intensity $I$. This effect can be seen from Eqs. (38) and (39). Indeed, larger $f$ does not change the magnitude of the fourth (destabilizing) term there (see the definitions of the parameters $M$, $T_s$, and $T_r$ in the Table), but it increases the stabilizing contribution of the last term. The inclusion in the model of weak evaporation and the corresponding recoil pressure at the free surface should partially reverse this trend.\(^{16}\)
near the equilibrium position the high-temperature regions makes the film surface stay low-temperature regions, while the strong heat generated in the high-temperature regions makes the film surface stay near the equilibrium position \( h = 1 \). The rupture time is 600 \( \mu s \), which is comparable to the time estimate given in Ref. 10 (>100 \( \mu s \) for a 10-nm-thick film). If the irradiation is stopped immediately after the first ruptures occur, the solidification that follows is expected to create the regular array of metallic ridges (nanowires) with the axes along the \( y \)-direction. In contrast to Fig. 9 where the irradiation is uniform, here the ridges have different volume, with the large (small) volume in the cold (hot) regions. Thus the ridges volume distribution has the period \( \ell \) of the interference imprint. This distribution is qualitatively consistent with the PLII experiments and modeling. Since the bulk film temperature is higher for thicker films (Fig. 8), then increasing the film height from 10 nm to 15 nm eliminates most ridges, except the one in the destructive regions. Nevertheless, the stabilizing effect of the internal heat generation becomes smaller as more heat is generated in thicker films.

f as in Eq. (43). Figure 12 shows the film profile after the two-beam irradiation, together with the interference field profile, i.e., the function \( f(x) \). Values of the parameters are \( \alpha = 0.99, q = 0.157, \) and \( k = 2.2 \). The ruptures first occur in the low-temperature regions, while the strong heat generated in the high-temperature regions makes the film surface stay near the equilibrium position \( h = 1 \). The rupture time is 600 \( \mu s \), which is comparable to the time estimate given in Ref. 10 (>100 \( \mu s \) for a 10-nm-thick film). If the irradiation is stopped immediately after the first ruptures occur, the solidification that follows is expected to create the regular array of metallic ridges (nanowires) with the axes along the \( y \)-direction. In contrast to Fig. 9 where the irradiation is uniform, here the ridges have different volume, with the large (small) volume in the cold (hot) regions. Thus the ridges volume distribution has the period \( \ell \) of the interference imprint. This distribution is qualitatively consistent with the PLII experiments and modeling.  

Finally, in Fig. 13 we plot the ratio of the rupture times, \( T_{r}^{(R \neq 0)}/T_{r}^{(R = 0)} \) vs. \( D \) for the case (TBC2). The simulations were done, in each case, with the most dangerous wave number \( k_{m} \) (for \( R = 0 \) and \( R \neq 0 \) the most dangerous wave numbers are different). It can be seen that this ratio is less than one for all values of \( D \) and changes nonmonotonously with \( D \), decreasing first and then increasing. The minimum value is as small as \( \sim 10^{-2} \). The ratio is less than one because the reflectivity reduces the heat generation in the film [Eq. (5)], thus reducing the stabilization. Note that, since the simulation is started with the small surface deformation (such that the predictions of the linear stability theory are valid for at least some time), the ratio does not give meaningful comparison in the interval \( D \sim 1 \). This is because the surface is linearly stable for \( R = 0 \) and \( R \neq 0 \) when \( D \sim 1 \), as shown in Fig. 7, and both \( T_{r}^{(R = 0)} \) and \( T_{r}^{(R \neq 0)} \) are formally infinite. Thus the ratio is not plotted for \( 0.085 \leq D \leq 4.1 \).

IV. DISCUSSION AND CONCLUSIONS

In this paper we study the dewetting dynamics of a pulsed-laser-irradiated metallic films. A lubrication-type model describing the flow of a molten film and the heat conduction in the film is developed. The heat absorbed from the laser beam is included as a source term in the heat conduction problem and the temperature field distribution in the film is obtained by solving this problem analytically. In the laser interference mode of irradiation, we observe that the lateral temperature distribution in the film mimics the shape of the lateral power intensity distribution of the laser. The temperature difference across the film and the temperature in the film are higher for optically thick films than for the optically thin ones.

The temperature field is used to derive the 3D long-wave evolution PDE for the film height. In order to get clear understandings of the film dynamics, we study the 2D version of the equation by means of the linear stability analysis and numerical simulations. The linearized problem allows us to investigate the stabilizing and destabilizing effects of various system parameters. Higher peak intensity of the beam and larger Marangoni number \( M \) either delay the rupture time of an initially perturbed film or make the perturbation decay, while smaller surface Biot number \( \beta \) and substrate Biot number \( \beta_{s} \), have the same effect. The increasing optical thickness \( D \) can have either stabilizing or destabilizing effect, depending on the magnitudes of the film reflectivity and the ratio of the substrate to film thermal conductivities. As film becomes thinner, the stabilizing effect of the internal heat generation becomes smaller as more heat is generated in thicker films. Impacts of the different modes of irradiation are investigated numerically in the 2D setting. For the spatially uniform (single beam) irradiation the film rupture is spatially periodic...
with the wavelength of the fastest growing perturbation. The latter wavelength is determined by values of all system parameters, including the laser parameters. In the two-beam interference heating mode the ruptures occur in the (cold) regions of destructive interference, while at the (hot) regions of constructive interference the initial surface perturbation is still developing. Assuming the irradiation is stopped after the first ruptures, the solidification is expected to create a ridge (nanowire) array, where the spatial distribution of ridges volumes follows the spatial periodicity of the interference imprint.

These conclusions do not depend, at large, on the presence of the thickness-dependent reflectivity. However, quite unexpectedly we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.

Finally, we point out the difference of thermocapillary mechanisms with and without heat generation in the film due to laser beam irradiation of the film surface. In standard applications, when the substrate is heated up to laser beam irradiation of the film surface. In standard applications, with and without heat generation in the film due to the one of the nonreflective films. Films having nonzero reflectivity is significantly shorter than the corresponding nonreflective films can be completely stabilized against dewetting and rupture, although quite unexpected we found that reflective films with $D \sim 1$ can be completely stabilized against dewetting and rupture, although films with $D$ either small or large are less stable than the corresponding nonreflective films (due to smaller magnitudes of the heat source in the reflective films). The rupture time from the simulations is comparable to the estimated and the experimentally obtained values. The rupture time of the films having nonzero reflectivity is significantly shorter than the one of the nonreflective films.